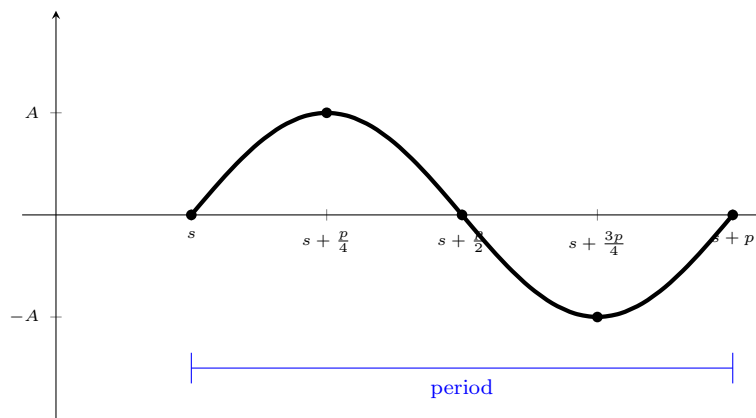


## Graphing Sine

Suppose we want to graph  $y = A \sin(Bx - C)$ , where  $A, B, C \neq 0$ . For the time being, assume that all three are positive. Then the amplitude is  $A$ , the period is  $\frac{2\pi}{B}$ , and the phase shift is  $\frac{C}{B}$ . Let's also let  $p = \frac{2\pi}{B}$  be the period and  $s = \frac{C}{B}$  be the phase shift. The graph of one period of  $y = A \sin(Bx - C)$  will always look like below (of course, you can choose a different period of the function to draw, but this seems the most natural to the author).

The  $x$ -intercepts will always occur at the points  $x = s, s + \frac{p}{2}, s + p$ , and the maxima/minima will always occur at the points  $x = s + \frac{p}{4}, s + \frac{3p}{4}$ . By plotting these five points, you can get a pretty accurate graph of  $y = A \sin(Bx - C)$ .

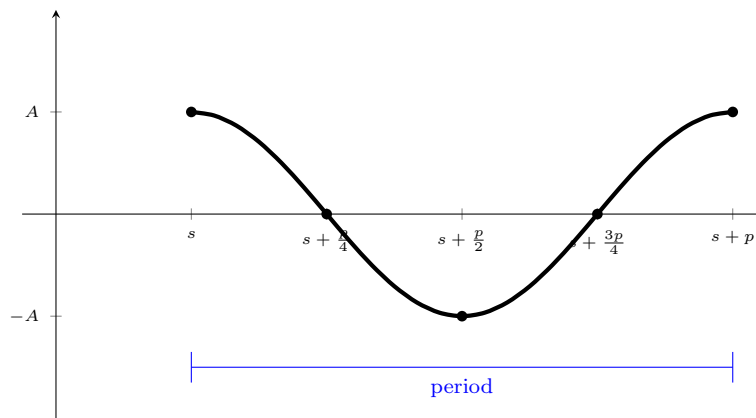


Of course, if  $A < 0$ , your graph will be the same as above, but reflected across the  $x$ -axis, and if  $C < 0$ , your shift will be to the left by  $s$  units.

## Graphing Cosine

Suppose we want to graph  $y = A \cos(Bx - C)$ , where  $A, B, C \neq 0$ . For the time being, assume that all three are positive. Then the amplitude is  $A$ , the period is  $\frac{2\pi}{B}$ , and the phase shift is  $\frac{C}{B}$ . Let's also let  $p = \frac{2\pi}{B}$  be the period and  $s = \frac{C}{B}$  be the phase shift. The graph of one period of  $y = A \cos(Bx - C)$  will always look like below (of course, you can choose a different period of the function to draw, but this seems the most natural to the author).

The  $x$ -intercepts will always occur at the points  $x = s + \frac{p}{4}, s + \frac{3p}{4}$ , and the maxima/minima will always occur at the points  $x = s, s + \frac{p}{2}, s + p$ . By plotting these five points, you can get a pretty accurate graph of  $y = A \cos(Bx - C)$ .



Of course, if  $A < 0$ , your graph will be the same as above, but reflected across the  $x$ -axis, and if  $C < 0$ , your shift will be to the left by  $s$  units.